

Problem:

Given a set of US Stock Market prices, $Z(t)$ for $t = 0$ to n , predict the value of $Z(t+1)$.

Data Source:

Tradestation: <http://www.tradestation.com/>

Stocks: S&P 500

Metrics: Open, Close, High, Low and Volume

Timeframe: January 1993, October 2013 (~20 years)

Total samples: ~3,650,000 (500 stocks * 365 days * 20 years)

Methods:

Statistical Learning: Bayesian Inference

- Given: $X(t) = \frac{Z(t) - Z(t-1)}{Z(t-1)} * 100$ where t spans from January 1st to December 31st of a given year. Compute the distribution from the observations for that year. At the end, there will be up to 20 different distributions.
- Given the sample $Y(t)$, use The Bayesian Classifier to classify which distribution (from step 1) most likely contains $Y(t)$.

$$\frac{P(w_1)P(X|w_1)}{P(w_2)P(X|w_2)} < (>) 1$$
- From sample $Y(t)$ and observations $X(t)$, compute the expected value for $Y(t+1)$:

$$\rho = \frac{E\{(X_t - \mu_x)(Y_{(t+1)} - \mu_y)\}}{\sigma_x \sigma_y}$$
 with $\rho = 0.3$ [or the correct value for the classified distribution].

Consensus: RANSAC

- Given observations $X(t)$ for $t = 0$ to n , select a random subset to fit a model.
- Repeat step 1, k times until the best model is chosen. k can be computed as:

$$k = \frac{\log(1-p)}{\log(1-w^n)}$$

- Using the consensus set, estimate the value for $X(t+1)$.

Context-Dependent Learning: Hidden Markov Models (discrete observation)

- Use Vector Quantization to categorize each observation into one of L possible distinct values in an l -dimensional space.
- Use Baum-Welch Reestimation to compute the parameters of model S . Thus $p(X|S)$ is the maximum likelihood estimator:

$$\mathfrak{I}_k(i, j) \equiv \mathfrak{I}_k(i, j, X|S) \equiv \frac{\mathfrak{I}_k(i, j, X|S)}{P(X|S)}$$

- Using Expectation Maximization, compute $X(t+1)$ such that the M (*maximization*) step is:

$$\Theta(t+1): \frac{\partial Q(\Theta; \Theta(t))}{\partial \Theta}$$

If time permits: attempt using the above algorithms in combination as an ensemble classifier to achieve even greater performance.

Validation:

The daily values extracted from Tradestation also include a 501st stock known as the SPDR (Spider). This ETF mimics the entire S&P. Thus the error can be computed as:

$\sqrt{(Z(t+1) - SPDR(t+1))^2}$. Furthermore, with 20 years of data, the set can easily be partitioned for K folds cross validation where each fold is between 4 and 10 years for $K = 2$ to 5.